

Unit 8 - Solubility Equilibrium (K_{sp})

Chapter 16

Review the following:

- Polyatomic ions and solubility rules
- Equilibrium constant expressions
- ICE charts
- Reaction quotient, Q
- Le Chatelier's Principle (shifts)
- $\text{pH} = -\log [\text{H}^+]$
- $\text{pOH} = -\log [\text{OH}^-]$
- $\text{pH} + \text{pOH} = 14$
- $[\text{H}^+] = 10^{-\text{pH}}$
- $[\text{OH}^-] = 10^{-\text{pOH}}$

Things to consider:

- Insoluble salts are actually slightly soluble
- Slightly soluble salts establish a dynamic equilibrium with the hydrated cations and anions in solution
 - When solid is first added to water, no ions are initially present in water
 - As dissolution proceeds, the concentration of ions increases until equilibrium is established (**equilibrium = saturated solution**)
- The presence of a **common ion** in solution **will reduce the molar solubility** of a salt
 - Occurs when a salt is dissolved in a solution that already contains the cations and/or anions of the salt being dissolved
- Q is used to determine whether a precipitate forms
 - $K_{sp} > Q$, the system is not at equilibrium (unsaturated), shift forward
 - $K_{sp} = Q$, the system is at equilibrium (saturated), no shift
 - $K_{sp} < Q$, the system is not at equilibrium (supersaturated), shift reverse

Precipitate forms when $K_{sp} < Q$. Concentrations of dissolved ions (the products) too high, causes reverse shift, thus precipitate (the reactant) forms.

4 Main Types of K_{sp} Problems:

1. Calculate molar solubility. Molar solubility is "x" from a K_{sp} ICE chart.
2. Calculate K_{sp}. Plug-in equilibrium values into K_{sp} expression and calculate.
3. Will a precipitate form? Calculate Q. Compare Q to K_{sp}. Determine direction of shift.
4. Which salt precipitates first? Calculate the equilibrium ion concentration needed to start precipitation of each salt. Whichever salt requires the lowest equilibrium ion concentration is the first to precipitate.

Problems:

1. AgCl(s) dissolves in water according to the equation below and has a K_{sp} value of 1.8×10^{-10} .
$$\text{AgCl}(s) \leftrightarrow \text{Ag}^+(aq) + \text{Cl}^-(aq)$$
 - a. Write the K_{sp} expression for the dissolution of AgCl(s).
 - b. What is the molar solubility of AgCl(s) in water?
2. The K_{sp} of CaF₂ is 4.0×10^{-11} . Calculate the molar solubility of CaF₂(s) in each of the following.
 - a. Pure water
 - b. 0.025 M NaF(aq)
 - c. Calculate the solubility, in grams per liter, of CaF₂(s) in the solution in part (b).

3. The K_{sp} of $\text{Fe}(\text{OH})_2(\text{s})$ is 8.0×10^{-16} . Calculate the molar solubility of $\text{Fe}(\text{OH})_2(\text{s})$ in each of the following.
 - a. Pure water
 - b. $0.010 \text{ M Fe}(\text{NO}_3)_2(\text{aq})$
 - c. $0.020 \text{ M NaOH}(\text{aq})$
4. Copper(I) bromide has a molar solubility of $2.0 \times 10^{-4} \text{ M}$ at 25°C . Calculate the K_{sp} of copper(I) bromide.
5. $\text{Bi}_2\text{S}_3(\text{s})$ has a molar solubility of $1.0 \times 10^{-15} \text{ M}$ at 25°C . Calculate the K_{sp} of $\text{Bi}_2\text{S}_3(\text{s})$.
6. A saturated solution of $\text{Mg}(\text{OH})_2$ has a pH of 10.36. Calculate the K_{sp} of $\text{Mg}(\text{OH})_2(\text{s})$.
7. A saturated solution of $\text{Cd}(\text{OH})_2$ has a pH of 9.333. Calculate the K_{sp} of $\text{Cd}(\text{OH})_2(\text{s})$.
8. 20.0 mL of $0.100 \text{ M Fe}(\text{NO}_3)_2(\text{aq})$ is mixed with 40.0 mL of $0.0500 \text{ M NaOH}(\text{aq})$. Will a precipitate of $\text{Fe}(\text{OH})_2$ form? The K_{sp} of $\text{Fe}(\text{OH})_2(\text{s})$ is 8.0×10^{-16} .
9. 0.100 L of $1.5 \times 10^{-3} \text{ M MgCl}_2(\text{aq})$ and 0.200 L of $0.025 \text{ M NaF}(\text{aq})$ are mixed. Will a precipitate of MgF_2 form? The K_{sp} of $\text{MgF}_2(\text{s})$ is 3.7×10^{-8} .
10. Will a precipitate of Ag_2CrO_4 form when 1.00 mg of $\text{Na}_2\text{CrO}_4(\text{s})$ is added to 225 mL of $1.5 \times 10^{-4} \text{ M AgNO}_3(\text{aq})$? The K_{sp} of $\text{Ag}_2\text{CrO}_4(\text{s})$ is 1.1×10^{-12} .
11. 20.0 mL of a $0.0100 \text{ M Mg}(\text{NO}_3)_2$ is mixed with 10.0 mL of a 0.0010 M ZnCl_2 . Sodium hydroxide solution is then slowly added to the mixture. Assume no volume change with the addition of sodium hydroxide.
 - a) Which salt, $\text{Mg}(\text{OH})_2$ ($K_{sp} = 6.0 \times 10^{-12}$) or $\text{Zn}(\text{OH})_2$ ($K_{sp} = 4.0 \times 10^{-17}$) will precipitate first?
 - b) What is the hydroxide concentration when the first precipitate begins to form?
12. A solution is 0.045 M in NaCl and 0.045 M in NaBr . Solid lead(II) nitrate is added without changing the volume of the solution.
 - a. Which salt, PbBr_2 ($K_{sp} = 6.6 \times 10^{-6}$) or PbCl_2 ($K_{sp} = 1.7 \times 10^{-5}$) will precipitate first?
 - b. What is the $[\text{Pb}^{2+}]$ when the first salt begins to precipitate?
13. A solution is 0.035 M in Na_2SO_4 and 0.035 M in Na_2CrO_4 . Solid lead(II) nitrate is added without changing the volume of the solution.
 - a. Which salt, PbSO_4 ($K_{sp} = 1.8 \times 10^{-8}$) or PbCrO_4 ($K_{sp} = 2.0 \times 10^{-14}$) will precipitate first?
 - b. What is the $[\text{Pb}^{2+}]$ when the salt in "a" first begins to precipitate?
14. A 65 mL solution of $0.40 \text{ M Al}(\text{NO}_3)_3$ is mixed with 125 mL of 0.17 M iron(II) nitrate. Solid sodium hydroxide is then added without changing the volume.
 - a. Which will precipitate first, $\text{Al}(\text{OH})_3$ ($K_{sp} = 2 \times 10^{-31}$) or $\text{Fe}(\text{OH})_2$ ($K_{sp} = 5 \times 10^{-17}$)?
 - b. What is the $[\text{OH}^-]$ when the first compound begins to precipitate?

Ksp Equilibrium HW WS

- Copper (II) sulfide has a K_{sp} of 1.0×10^{-36} . What is the molar solubility in moles per liter of copper (II) sulfide in
 - 0.020M copper (II) sulfate solution?
 - 0.010 M sodium sulfide solution?
- $Mg_3(PO_4)_2$ has a K_{sp} of 1.0×10^{-24} . What is the molar solubility in grams per liter of magnesium phosphate in
 - 0.010M sodium phosphate solution?
 - 0.030M magnesium nitrate solution?
- Calculate the $[OH^-]$ in equilibrium with $1.00 \times 10^{-4} M Zn^{+2}$ if the K_{sp} of $Zn(OH)_2$ is 4.0×10^{-17} ?
- What is the pH of the solution in question #3
- Silver nitrate is added to a solution of $2.00 \times 10^{-2} M$ sodium phosphate. What is the equilibrium concentration of Ag^+ ? (K_{sp} of silver phosphate is 1.0×10^{-16})
- Lead (II) chromate, $PbCrO_4$, is the yellow paint pigment known as "chrome yellow". A solution is prepared by mixing a solution that is $1.0 \times 10^{-4} M$ in lead (II) ion with a solution that is $5.0 \times 10^{-3} M$ in chromate ion. Ignoring dilution effects, would a precipitate form? The K_{sp} of lead (II) chromate is 2.0×10^{-14} ?
- A solution is prepared by mixing 25.0 mL of 0.100 M iron(II) nitrate with 50.0 mL of a sodium hydroxide solution of pH 9.00. Will a precipitate form? The K_{sp} of iron(II) hydroxide is 5.0×10^{-17} ?

Answers: 1a) $5.0 \times 10^{-35} M$ 1b) $1.0 \times 10^{-34} M$ 2a) $1.89 \times 10^{-5} g/L$ 2b) $2.53 \times 10^{-8} g/L$ 3) $6.32 \times 10^{-7} M$
4) 7.801 5) $1.71 \times 10^{-5} M$ 6) $Q=5.0 \times 10^{-7}$, thus a ppt will form 7) $Q=1.47 \times 10^{-12}$, thus a ppt will form